

HOMEWORK 5-PART A

- (1) Write down the augmented matrix for the system.
- (2) Solve the solutions of following linear equation system in terms of parametric form. And draw the solution in xyz-space.

$$\begin{aligned}x - 3y + 4z &= 12, \\ -3x + 10y + 8z &= 40\end{aligned}$$

- (1) How many possibilities of solutions for the case—"three linear equations in three variables"?
- (2) Solve the following linear equation system:

$$\begin{aligned}x - y + 2z &= 4 \\ -2x + y - z &= 6 \\ 3x + y - 3z &= 7\end{aligned}$$

- For an $n \times n$ matrix A , the trace of A is defined as the sum of diagonal entries of A . e.g. For $A = \begin{pmatrix} 2 & 1 \\ 1 & 3 \end{pmatrix}$, then trace of A equals to $2 + 3 = 5$.

- (1) Now please calculate trace of AB and trace of BA , for $A = \begin{pmatrix} 2 & 1 & 5 \\ 1 & 3 & 7 \\ 2 & 1 & 2 \end{pmatrix}$

and $B = \begin{pmatrix} 9 & 2 & 1 \\ 0 & 1 & 3 \\ 2 & 0 & 8 \end{pmatrix}$. Comparing both, what can you say?

- (2) Calculate trace of A and trace of A^T , comparing both, what can you say?