## Math 222 in class problems

Week: March 1, 2021

1. Evaluate

$$\int_{-2}^{2} \int_{-\sqrt{4-x^2}}^{\sqrt{4-x^2}} \int_{\sqrt{x^2+y^2}}^{2} x^2 + y^2 dz dy dx$$

- 2. Find the volume of the region lying between the planes z=0 and z=4-x, outside the cylinder with base  $r=2\cos\theta$ , and inside the cylinder with base  $(x-2)^2+y^2=4$ .
- 3. Set up the integral representing the volume of the solid region bounded between z=4,  $z=1-x^2-y^2$ , which is inside  $x^2+y^2=1$ .
- 4. HW #5 4b)

Sketch the solid whose volume is given by the integral and evaluate the integral

$$\int_0^{\pi/4} \int_0^{2\pi} \int_0^{\sec \varphi} \rho^2 \sin \varphi \ d\rho \ d\theta \ d\varphi$$

5. Graph the region of integration and convert to spherical coordinates in order to evaluate (but do not do so):

$$\int_0^3 \int_0^{\sqrt{9-y^2}} \int_{\sqrt{x^2+y^2}}^{\sqrt{18-x^2-y^2}} x^2 + y^2 + z^2 dz dx dy$$